

# C1. Listing of Utility Modules (nrtype and nrutil)

## C1.1 Numerical Recipes Types (nrtype)

The file supplied as nrtype.f90 contains a single module named nrtype, which in turn contains definitions for a number of named constants (that is, PARAMETERS), and a couple of elementary derived data types used by the sparse matrix routines in this book. Of the named constants, by far the most important are those that define the KIND types of virtually all the variables used in this book: I4B, I2B, and I1B for integer variables, SP and DP for real variables (and SPC and DPC for the corresponding complex cases), and LGT for the default logical type.

### MODULE nrtype

Symbolic names for kind types of 4-, 2-, and 1-byte integers:

```
INTEGER, PARAMETER :: I4B = SELECTED_INT_KIND(9)
INTEGER, PARAMETER :: I2B = SELECTED_INT_KIND(4)
INTEGER, PARAMETER :: I1B = SELECTED_INT_KIND(2)
```

Symbolic names for kind types of single- and double-precision reals:

```
INTEGER, PARAMETER :: SP = KIND(1.0)
INTEGER, PARAMETER :: DP = KIND(1.0D0)
```

Symbolic names for kind types of single- and double-precision complex:

```
INTEGER, PARAMETER :: SPC = KIND((1.0,1.0))
INTEGER, PARAMETER :: DPC = KIND((1.0D0,1.0D0))
```

Symbolic name for kind type of default logical:

```
INTEGER, PARAMETER :: LGT = KIND(.true.)
```

Frequently used mathematical constants (with precision to spare):

```
REAL(SP), PARAMETER :: PI=3.141592653589793238462643383279502884197_sp
REAL(SP), PARAMETER :: PI02=1.57079632679489661923132169163975144209858_sp
REAL(SP), PARAMETER :: TWOPI=6.283185307179586476925286766559005768394_sp
REAL(SP), PARAMETER :: SQRT2=1.41421356237309504880168872420969807856967_sp
REAL(SP), PARAMETER :: EULER=0.5772156649015328606065120900824024310422_sp
REAL(DP), PARAMETER :: PI_D=3.141592653589793238462643383279502884197_dp
REAL(DP), PARAMETER :: PI02_D=1.57079632679489661923132169163975144209858_dp
REAL(DP), PARAMETER :: TWOPI_D=6.283185307179586476925286766559005768394_dp
```

Derived data types for sparse matrices, single and double precision (see use in Chapter B2):

```
TYPE sprs2_sp
  INTEGER(I4B) :: n,len
  REAL(SP), DIMENSION(:), POINTER :: val
  INTEGER(I4B), DIMENSION(:), POINTER :: irow
  INTEGER(I4B), DIMENSION(:), POINTER :: jcol
END TYPE sprs2_sp
TYPE sprs2_dp
  INTEGER(I4B) :: n,len
  REAL(DP), DIMENSION(:), POINTER :: val
```

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```

INTEGER(I4B), DIMENSION(:), POINTER :: irow
INTEGER(I4B), DIMENSION(:), POINTER :: jcol
END TYPE sprs2_dp
END MODULE nrtype

```

## About Converting to Higher Precision

You might hope that changing all the Numerical Recipes routines from single precision to double precision would be as simple as redefining the values of SP and DP in *nrtype*. Well . . . not quite.

Converting algorithms to a higher precision is not a purely mechanical task because of the distinction between “roundoff error” and “truncation error.” (Please see Volume 1, §1.2, if you are not familiar with these concepts.) While increasing the precision implied by the kind values SP and DP will indeed reduce a routine’s roundoff error, it will not reduce any truncation error that may be intrinsic to the algorithm. Sometimes, a routine contains “accuracy parameters” that can be adjusted to reduce the truncation error to the new, desired level. In other cases, however, the truncation error cannot be so easily reduced; then, a whole new algorithm is needed. Clearly such new algorithms are beyond the scope of a simple mechanical “conversion.”

If, despite these cautionary words, you want to proceed with converting some routines to a higher precision, here are some hints:

If your machine has a kind type that is distinct from, and has equal or greater precision than, the kind type that we use for DP, then, in *nrtype*, you can simply redefine DP to this new highest precision and redefine SP to what was previously DP. For example, DEC machines usually have a “quadruple precision” real type available, which can be used in this way. You should not need to make any further edits of *nrtype* or *nrutil*.

If, on the other hand, the kind type that we already use for DP is the highest precision available, then you must leave DP defined as it is, and redefine SP in *nrtype* to be this same kind type. Now, however, you will also have to edit *nrutil*, because some overloaded routines that were previously distinguishable (by the different kind types) will now be seen by the compiler as indistinguishable — and it will object strenuously. Simply delete all the “\_dp” function names from the list of overloaded procedures (i.e., from the MODULE PROCEDURE statements). Note that it is not necessary to delete the routines from the MODULE itself. Similarly, in the interface file *nr.f90* you must delete the “\_dp” interfaces, *except* for the *sprs* . . . routines. (Since they have TYPE(*sprs2\_dp*) or TYPE(*sprs2\_sp*), they are treated as distinct even though they have functionally equivalent kind types.)

Finally, the following table gives some suggestions for changing the accuracy parameters, or constants, in some of the routines. Please note that this table is not necessarily complete, and that higher-precision performance is not guaranteed for all the routines, *even if* you make all the changes indicated. The above edits, and these suggestions, do, however, work in the majority of cases.

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<i>In routine...</i>	<i>change...</i>	<i>to...</i>
beschb	NUSE1=5,NUSE2=5	NUSE1=7,NUSE2=8
bessi	IACC=40	IACC=200
bessik	EPS=1.0e-10 <sub>dp</sub>	EPS=epsilon(x)
bessj	IACC=40	IACC=160
bessjy	EPS=1.0e-10 <sub>dp</sub>	EPS=epsilon(x)
broydn	TOLF=1.0e-4 <sub>sp</sub> TOLMIN=1.0e-6 <sub>sp</sub>	TOLF=1.0e-8 <sub>sp</sub> TOLMIN=1.0e-12 <sub>sp</sub>
fdjac	EPS=1.0e-4 <sub>sp</sub>	EPS=1.0e-8 <sub>sp</sub>
frprmn	EPS=1.0e-10 <sub>sp</sub>	EPS=1.0e-18 <sub>sp</sub>
gauher	EPS=3.0e-13 <sub>dp</sub>	EPS=1.0e-14 <sub>dp</sub>
gaujac	EPS=3.0e-14 <sub>dp</sub>	EPS=1.0e-14 <sub>dp</sub>
gaulag	EPS=3.0e-13 <sub>dp</sub>	EPS=1.0e-14 <sub>dp</sub>
gauleg	EPS=3.0e-14 <sub>dp</sub>	EPS=1.0e-14 <sub>dp</sub>
hypgeo	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-14 <sub>sp</sub>
linmin	TOL=1.0e-4 <sub>sp</sub>	TOL=1.0e-8 <sub>sp</sub>
newt	TOLF=1.0e-4 <sub>sp</sub> TOLMIN=1.0e-6 <sub>sp</sub>	TOLF=1.0e-8 <sub>sp</sub> TOLMIN=1.0e-12 <sub>sp</sub>
probks	EPS1=0.001 <sub>sp</sub> EPS2=1.0e-8 <sub>sp</sub>	EPS1=1.0e-6 <sub>sp</sub> EPS2=1.0e-16 <sub>sp</sub>
qromb	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-10 <sub>sp</sub>
qromo	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-10 <sub>sp</sub>
qroot	TINY=1.0e-6 <sub>sp</sub>	TINY=1.0e-14 <sub>sp</sub>
qsimp	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-10 <sub>sp</sub>
qtrap	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-10 <sub>sp</sub>
rc	ERRTOL=0.04 <sub>sp</sub>	ERRTOL=0.0012 <sub>sp</sub>
rd	ERRTOL=0.05 <sub>sp</sub>	ERRTOL=0.0015 <sub>sp</sub>
rf	ERRTOL=0.08 <sub>sp</sub>	ERRTOL=0.0025 <sub>sp</sub>
rj	ERRTOL=0.05 <sub>sp</sub>	ERRTOL=0.0015 <sub>sp</sub>
sfroid	conv=5.0e-6 <sub>sp</sub>	conv=1.0e-14 <sub>sp</sub>
shoot	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-14 <sub>sp</sub>
shootf	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-14 <sub>sp</sub>
simplx	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-14 <sub>sp</sub>
sncndn	CA=0.0003 <sub>sp</sub>	CA=1.0e-8 <sub>sp</sub>
sor	EPS=1.0e-5 <sub>dp</sub>	EPS=1.0e-13 <sub>dp</sub>
sphfpt	DXX=1.0e-4 <sub>sp</sub>	DXX=1.0e-8 <sub>sp</sub>
sphoot	dx=1.0e-4 <sub>sp</sub>	dx=1.0e-8 <sub>sp</sub>
svdfit	TOL=1.0e-5 <sub>sp</sub>	TOL=1.0e-13 <sub>sp</sub>
zroots	EPS=1.0e-6 <sub>sp</sub>	EPS=1.0e-14 <sub>sp</sub>

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## C1.2 Numerical Recipes Utilities (*nrutil*)

The file supplied as `nrutil.f90` contains a single module named `nrutil`, which contains specific implementations for all the Numerical Recipes utility functions described in detail in Chapter 23.

The specific implementations given are something of a compromise between demonstrating parallel techniques (when they can be achieved in Fortran 90) and running efficiently on conventional, serial machines. The parameters at the beginning of the module (names beginning with `NPAR_`) are typically related to array lengths *below which* the implementations revert to serial operations. On a purely serial machine, these can be set to large values to suppress many parallel constructions.

The length and repetitiveness of the `nrutil.f90` file stems in large part from its extensive use of overloading. Indeed, the file would be even longer if we overloaded versions for all the applicable data types that each utility could, in principle, instantiate. The descriptions in Chapter 23 detail both the full set of intended data types and shapes for each routine, and also the types and shapes actually here implemented (which can also be gleaned by examining the file). The intended result of all this overloading is, in essence, to give the utility routines the desirable properties of many of the Fortran 90 intrinsic functions, namely, to be both *generic* (apply to many data types) and *elemental* (apply element-by-element to arbitrary shapes). Fortran 95's provision of user-defined elemental functions will reduce the multiplicity of overloading in some of our routines; unfortunately the necessity to overload for multiple data types will still be present.

Finally, it is worth reemphasizing the following point, already made in Chapter 23: The purpose of the `nrutil` utilities is to remove from the Numerical Recipes programs just those programming tasks and "idioms" whose efficient implementation is *most* hardware and compiler dependent, so as to allow for specific, efficient implementations on different machines. One should therefore not expect the utmost in efficiency from the general purpose, one-size-fits-all, implementation listed here.

Correspondingly, we would encourage the incorporation of efficient `nrutil` implementations, and/or comparable capabilities under different names, with as broad as possible a set of overloaded data types, in libraries associated with specific compilers or machines. In support of this goal, we have specifically put this Appendix C1, and the files `nrtype.f90` and `nrutil.f90`, into the public domain.

### MODULE `nrutil`

#### TABLE OF CONTENTS OF THE NRUTIL MODULE:

- routines that move data:
  - `array_copy`, `swap`, `reallocate`
- routines returning a location as an integer value
  - `ifirstloc`, `imaxloc`, `iminloc`
- routines for argument checking and error handling:
  - `assert`, `assert_eq`, `nrerror`
- routines relating to polynomials and recurrences
  - `arth`, `geop`, `cumsum`, `cumprod`, `poly`, `polyterm`, `zroots_unity`
- routines for "outer" operations on vectors
  - `outerand`, `outersum`, `outerdiff`, `outerprod`, `outerdiv`
- routines for scatter-with-combine
  - `scatter_add`, `scatter_max`
- routines for skew operations on matrices
  - `diagadd`, `diagmult`, `get_diag`, `put_diag`,

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```

        unit_matrix, lower_triangle, upper_triangle
miscellaneous routines
    vabs
USE nrtype
    Parameters for crossover from serial to parallel algorithms (these are used only within this
nrutil module):
IMPLICIT NONE
INTEGER(I4B), PARAMETER :: NPAR_ARTH=16,NPAR2_ARTH=8    Each NPAR2 must be ≤ the
INTEGER(I4B), PARAMETER :: NPAR_GEOP=4,NPAR2_GEOP=2    corresponding NPAR.
INTEGER(I4B), PARAMETER :: NPAR_CUMSUM=16
INTEGER(I4B), PARAMETER :: NPAR_CUMPROD=8
INTEGER(I4B), PARAMETER :: NPAR_POLY=8
INTEGER(I4B), PARAMETER :: NPAR_POLYTERM=8
    Next, generic interfaces for routines with overloaded versions. Naming conventions for ap-
    pended codes in the names of overloaded routines are as follows: r=real, d=double pre-
    cision, i=integer, c=complex, z=double-precision complex, h=character, l=logical. Any of
    r,d,i,c,z,h,l may be followed by v=vector or m=matrix (v,m suffixes are used only when
    needed to resolve ambiguities).
    Routines that move data:
INTERFACE array_copy
    MODULE PROCEDURE array_copy_r, array_copy_d, array_copy_i
END INTERFACE
INTERFACE swap
    MODULE PROCEDURE swap_i,swap_r,swap_rv,swap_c, &
        swap_cv,swap_cm,swap_z,swap_zv,swap_zm, &
        masked_swap_rs,masked_swap_rv,masked_swap_rm
END INTERFACE
INTERFACE reallocate
    MODULE PROCEDURE reallocate_rv,reallocate_rm,&
        reallocate_iv,reallocate_im,reallocate_hv
END INTERFACE
    Routines returning a location as an integer value (ifirstloc, iminloc are not currently over-
    loaded and so do not have a generic interface here):
INTERFACE imaxloc
    MODULE PROCEDURE imaxloc_r,imaxloc_i
END INTERFACE
    Routines for argument checking and error handling (nrerror is not currently overloaded):
INTERFACE assert
    MODULE PROCEDURE assert1,assert2,assert3,assert4,assert_v
END INTERFACE
INTERFACE assert_eq
    MODULE PROCEDURE assert_eq2,assert_eq3,assert_eq4,assert_eqn
END INTERFACE
    Routines relating to polynomials and recurrences (cumprod, zroots_unity are not currently
    overloaded):
INTERFACE arth
    MODULE PROCEDURE arth_r, arth_d, arth_i
END INTERFACE
INTERFACE geop
    MODULE PROCEDURE geop_r, geop_d, geop_i, geop_c, geop_dv
END INTERFACE
INTERFACE cumsum
    MODULE PROCEDURE cumsum_r,cumsum_i
END INTERFACE
INTERFACE poly
    MODULE PROCEDURE poly_rr,poly_rrv,poly_dd,poly_ddv,&
        poly_rc,poly_cc,poly_msk_rrv,poly_msk_ddv
END INTERFACE
INTERFACE poly_term
    MODULE PROCEDURE poly_term_rr,poly_term_cc
END INTERFACE
    Routines for “outer” operations on vectors (outerand, outersum, outerdiv are not currently
    overloaded):
INTERFACE outerprod

```

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```

MODULE PROCEDURE outerprod_r,outerprod_d
END INTERFACE
INTERFACE outerdiff
MODULE PROCEDURE outerdiff_r,outerdiff_d,outerdiff_i
END INTERFACE
Routines for scatter-with-combine, scatter_add, scatter_max:
INTERFACE scatter_add
MODULE PROCEDURE scatter_add_r,scatter_add_d
END INTERFACE
INTERFACE scatter_max
MODULE PROCEDURE scatter_max_r,scatter_max_d
END INTERFACE
Routines for skew operations on matrices (unit_matrix, lower_triangle, upper_triangle not
currently overloaded):
INTERFACE diagadd
MODULE PROCEDURE diagadd_rv,diagadd_r
END INTERFACE
INTERFACE diagmult
MODULE PROCEDURE diagmult_rv,diagmult_r
END INTERFACE
INTERFACE get_diag
MODULE PROCEDURE get_diag_rv, get_diag_dv
END INTERFACE
INTERFACE put_diag
MODULE PROCEDURE put_diag_rv, put_diag_r
END INTERFACE
Other routines (vabs is not currently overloaded):
CONTAINS
Routines that move data:
SUBROUTINE array_copy_r(src,dest,n_copied,n_not_copied)
Copy array where size of source not known in advance.
REAL(SP), DIMENSION(:), INTENT(IN) :: src
REAL(SP), DIMENSION(:), INTENT(OUT) :: dest
INTEGER(I4B), INTENT(OUT) :: n_copied, n_not_copied
n_copied=min(size(src),size(dest))
n_not_copied=size(src)-n_copied
dest(1:n_copied)=src(1:n_copied)
END SUBROUTINE array_copy_r

SUBROUTINE array_copy_d(src,dest,n_copied,n_not_copied)
REAL(DP), DIMENSION(:), INTENT(IN) :: src
REAL(DP), DIMENSION(:), INTENT(OUT) :: dest
INTEGER(I4B), INTENT(OUT) :: n_copied, n_not_copied
n_copied=min(size(src),size(dest))
n_not_copied=size(src)-n_copied
dest(1:n_copied)=src(1:n_copied)
END SUBROUTINE array_copy_d

SUBROUTINE array_copy_i(src,dest,n_copied,n_not_copied)
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: src
INTEGER(I4B), DIMENSION(:), INTENT(OUT) :: dest
INTEGER(I4B), INTENT(OUT) :: n_copied, n_not_copied
n_copied=min(size(src),size(dest))
n_not_copied=size(src)-n_copied
dest(1:n_copied)=src(1:n_copied)
END SUBROUTINE array_copy_i

SUBROUTINE swap_i(a,b)
Swap the contents of a and b.
INTEGER(I4B), INTENT(INOUT) :: a,b
INTEGER(I4B) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_i

```

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```

SUBROUTINE swap_r(a,b)
REAL(SP), INTENT(INOUT) :: a,b
REAL(SP) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_r

SUBROUTINE swap_rv(a,b)
REAL(SP), DIMENSION(:), INTENT(INOUT) :: a,b
REAL(SP), DIMENSION(SIZE(a)) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_rv

SUBROUTINE swap_c(a,b)
COMPLEX(SPC), INTENT(INOUT) :: a,b
COMPLEX(SPC) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_c

SUBROUTINE swap_cv(a,b)
COMPLEX(SPC), DIMENSION(:), INTENT(INOUT) :: a,b
COMPLEX(SPC), DIMENSION(SIZE(a)) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_cv

SUBROUTINE swap_cm(a,b)
COMPLEX(SPC), DIMENSION(:,:), INTENT(INOUT) :: a,b
COMPLEX(SPC), DIMENSION(size(a,1),size(a,2)) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_cm

SUBROUTINE swap_z(a,b)
COMPLEX(DPC), INTENT(INOUT) :: a,b
COMPLEX(DPC) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_z

SUBROUTINE swap_zv(a,b)
COMPLEX(DPC), DIMENSION(:), INTENT(INOUT) :: a,b
COMPLEX(DPC), DIMENSION(SIZE(a)) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_zv

SUBROUTINE swap_zm(a,b)
COMPLEX(DPC), DIMENSION(:,:), INTENT(INOUT) :: a,b
COMPLEX(DPC), DIMENSION(size(a,1),size(a,2)) :: dum
dum=a
a=b
b=dum
END SUBROUTINE swap_zm

SUBROUTINE masked_swap_rs(a,b,mask)
REAL(SP), INTENT(INOUT) :: a,b
LOGICAL(LGT), INTENT(IN) :: mask
REAL(SP) :: swp

```

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```

if (mask) then
  swp=a
  a=b
  b=swp
end if
END SUBROUTINE masked_swap_rs

SUBROUTINE masked_swap_rv(a,b,mask)
REAL(SP), DIMENSION(:), INTENT(INOUT) :: a,b
LOGICAL(LGT), DIMENSION(:), INTENT(IN) :: mask
REAL(SP), DIMENSION(size(a)) :: swp
where (mask)
  swp=a
  a=b
  b=swp
end where
END SUBROUTINE masked_swap_rv

SUBROUTINE masked_swap_rm(a,b,mask)
REAL(SP), DIMENSION(:, :), INTENT(INOUT) :: a,b
LOGICAL(LGT), DIMENSION(:, :), INTENT(IN) :: mask
REAL(SP), DIMENSION(size(a,1),size(a,2)) :: swp
where (mask)
  swp=a
  a=b
  b=swp
end where
END SUBROUTINE masked_swap_rm

FUNCTION reallocate_rv(p,n)
  Reallocate a pointer to a new size, preserving its previous contents.
REAL(SP), DIMENSION(:), POINTER :: p, reallocate_rv
INTEGER(I4B), INTENT(IN) :: n
INTEGER(I4B) :: nold,ierr
allocate(reallocate_rv(n),stat=ierr)
if (ierr /= 0) call &
  nrerror('reallocate_rv: problem in attempt to allocate memory')
if (.not. associated(p)) RETURN
nold=size(p)
reallocate_rv(1:min(nold,n))=p(1:min(nold,n))
deallocate(p)
END FUNCTION reallocate_rv

FUNCTION reallocate_iv(p,n)
INTEGER(I4B), DIMENSION(:), POINTER :: p, reallocate_iv
INTEGER(I4B), INTENT(IN) :: n
INTEGER(I4B) :: nold,ierr
allocate(reallocate_iv(n),stat=ierr)
if (ierr /= 0) call &
  nrerror('reallocate_iv: problem in attempt to allocate memory')
if (.not. associated(p)) RETURN
nold=size(p)
reallocate_iv(1:min(nold,n))=p(1:min(nold,n))
deallocate(p)
END FUNCTION reallocate_iv

FUNCTION reallocate_hv(p,n)
CHARACTER(1), DIMENSION(:), POINTER :: p, reallocate_hv
INTEGER(I4B), INTENT(IN) :: n
INTEGER(I4B) :: nold,ierr
allocate(reallocate_hv(n),stat=ierr)
if (ierr /= 0) call &
  nrerror('reallocate_hv: problem in attempt to allocate memory')
if (.not. associated(p)) RETURN
nold=size(p)
reallocate_hv(1:min(nold,n))=p(1:min(nold,n))

```

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```

deallocate(p)
END FUNCTION reallocate_hv

FUNCTION reallocate_rm(p,n,m)
REAL(SP), DIMENSION(:,:), POINTER :: p, reallocate_rm
INTEGER(I4B), INTENT(IN) :: n,m
INTEGER(I4B) :: nold,mold,ierr
allocate(reallocate_rm(n,m),stat=ierr)
if (ierr /= 0) call &
  nrerror('reallocate_rm: problem in attempt to allocate memory')
if (.not. associated(p)) RETURN
nold=size(p,1)
mold=size(p,2)
reallocate_rm(1:min(nold,n),1:min(mold,m))=&
  p(1:min(nold,n),1:min(mold,m))
deallocate(p)
END FUNCTION reallocate_rm

FUNCTION reallocate_im(p,n,m)
INTEGER(I4B), DIMENSION(:,:), POINTER :: p, reallocate_im
INTEGER(I4B), INTENT(IN) :: n,m
INTEGER(I4B) :: nold,mold,ierr
allocate(reallocate_im(n,m),stat=ierr)
if (ierr /= 0) call &
  nrerror('reallocate_im: problem in attempt to allocate memory')
if (.not. associated(p)) RETURN
nold=size(p,1)
mold=size(p,2)
reallocate_im(1:min(nold,n),1:min(mold,m))=&
  p(1:min(nold,n),1:min(mold,m))
deallocate(p)
END FUNCTION reallocate_im

```

Routines returning a location as an integer value:

```

FUNCTION ifirstloc(mask)
  Index of first occurrence of .true. in a logical vector.
LOGICAL(LGT), DIMENSION(:), INTENT(IN) :: mask
INTEGER(I4B) :: ifirstloc
INTEGER(I4B), DIMENSION(1) :: loc
loc=maxloc(merge(1,0,mask))
ifirstloc=loc(1)
if (.not. mask(ifirstloc)) ifirstloc=size(mask)+1
END FUNCTION ifirstloc

FUNCTION imaxloc_r(arr)
  Index of maxloc on an array.
REAL(SP), DIMENSION(:), INTENT(IN) :: arr
INTEGER(I4B) :: imaxloc_r
INTEGER(I4B), DIMENSION(1) :: imax
imax=maxloc(arr(:))
imaxloc_r=imax(1)
END FUNCTION imaxloc_r

FUNCTION imaxloc_i(iarr)
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: iarr
INTEGER(I4B), DIMENSION(1) :: imax
INTEGER(I4B) :: imaxloc_i
imax=maxloc(iarr(:))
imaxloc_i=imax(1)
END FUNCTION imaxloc_i

FUNCTION iminloc(arr)
  Index of minloc on an array.
REAL(SP), DIMENSION(:), INTENT(IN) :: arr
INTEGER(I4B), DIMENSION(1) :: imin
INTEGER(I4B) :: iminloc
imin=minloc(arr(:))

```

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```

iminloc=imin(1)
END FUNCTION iminloc

  Routines for argument checking and error handling:
SUBROUTINE assert1(n1,string)
  Report and die if any logical is false (used for arg range checking).
CHARACTER(LEN=*), INTENT(IN) :: string
LOGICAL, INTENT(IN) :: n1
if (.not. n1) then
  write (*,*) 'nrerror: an assertion failed with this tag:', &
    string
  STOP 'program terminated by assert1'
end if
END SUBROUTINE assert1

SUBROUTINE assert2(n1,n2,string)
CHARACTER(LEN=*), INTENT(IN) :: string
LOGICAL, INTENT(IN) :: n1,n2
if (.not. (n1 .and. n2)) then
  write (*,*) 'nrerror: an assertion failed with this tag:', &
    string
  STOP 'program terminated by assert2'
end if
END SUBROUTINE assert2

SUBROUTINE assert3(n1,n2,n3,string)
CHARACTER(LEN=*), INTENT(IN) :: string
LOGICAL, INTENT(IN) :: n1,n2,n3
if (.not. (n1 .and. n2 .and. n3)) then
  write (*,*) 'nrerror: an assertion failed with this tag:', &
    string
  STOP 'program terminated by assert3'
end if
END SUBROUTINE assert3

SUBROUTINE assert4(n1,n2,n3,n4,string)
CHARACTER(LEN=*), INTENT(IN) :: string
LOGICAL, INTENT(IN) :: n1,n2,n3,n4
if (.not. (n1 .and. n2 .and. n3 .and. n4)) then
  write (*,*) 'nrerror: an assertion failed with this tag:', &
    string
  STOP 'program terminated by assert4'
end if
END SUBROUTINE assert4

SUBROUTINE assert_v(n,string)
CHARACTER(LEN=*), INTENT(IN) :: string
LOGICAL, DIMENSION(:), INTENT(IN) :: n
if (.not. all(n)) then
  write (*,*) 'nrerror: an assertion failed with this tag:', &
    string
  STOP 'program terminated by assert_v'
end if
END SUBROUTINE assert_v

FUNCTION assert_eq2(n1,n2,string)
  Report and die if integers not all equal (used for size checking).
CHARACTER(LEN=*), INTENT(IN) :: string
INTEGER, INTENT(IN) :: n1,n2
INTEGER :: assert_eq2
if (n1 == n2) then
  assert_eq2=n1
else
  write (*,*) 'nrerror: an assert_eq failed with this tag:', &
    string
  STOP 'program terminated by assert_eq2'
end if

```

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```

END FUNCTION assert_eq2

FUNCTION assert_eq3(n1,n2,n3,string)
CHARACTER(LEN=*), INTENT(IN) :: string
INTEGER, INTENT(IN) :: n1,n2,n3
INTEGER :: assert_eq3
if (n1 == n2 .and. n2 == n3) then
  assert_eq3=n1
else
  write (*,*) 'nrerror: an assert_eq failed with this tag:', &
    string
  STOP 'program terminated by assert_eq3'
end if
END FUNCTION assert_eq3

FUNCTION assert_eq4(n1,n2,n3,n4,string)
CHARACTER(LEN=*), INTENT(IN) :: string
INTEGER, INTENT(IN) :: n1,n2,n3,n4
INTEGER :: assert_eq4
if (n1 == n2 .and. n2 == n3 .and. n3 == n4) then
  assert_eq4=n1
else
  write (*,*) 'nrerror: an assert_eq failed with this tag:', &
    string
  STOP 'program terminated by assert_eq4'
end if
END FUNCTION assert_eq4

FUNCTION assert_eqn(nn,string)
CHARACTER(LEN=*), INTENT(IN) :: string
INTEGER, DIMENSION(:), INTENT(IN) :: nn
INTEGER :: assert_eqn
if (all(nn(2:) == nn(1))) then
  assert_eqn=nn(1)
else
  write (*,*) 'nrerror: an assert_eq failed with this tag:', &
    string
  STOP 'program terminated by assert_eqn'
end if
END FUNCTION assert_eqn

SUBROUTINE nrerror(string)
  Report a message, then die.
CHARACTER(LEN=*), INTENT(IN) :: string
write (*,*) 'nrerror: ',string
STOP 'program terminated by nrerror'
END SUBROUTINE nrerror

Routines relating to polynomials and recurrences:
FUNCTION arth_r(first,increment,n)
  Array function returning an arithmetic progression.
REAL(SP), INTENT(IN) :: first,increment
INTEGER(I4B), INTENT(IN) :: n
REAL(SP), DIMENSION(n) :: arth_r
INTEGER(I4B) :: k,k2
REAL(SP) :: temp
if (n > 0) arth_r(1)=first
if (n <= NPAR_ARTH) then
  do k=2,n
    arth_r(k)=arth_r(k-1)+increment
  end do
else
  do k=2,NPAR2_ARTH
    arth_r(k)=arth_r(k-1)+increment
  end do
  temp=increment*NPAR2_ARTH
  k=NPAR2_ARTH

```

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```

do
  if (k >= n) exit
  k2=k+k
  arth_r(k+1:min(k2,n))=temp+arth_r(1:min(k,n-k))
  temp=temp+temp
  k=k2
end do
end if
END FUNCTION arth_r

FUNCTION arth_d(first,increment,n)
REAL(DP), INTENT(IN) :: first,increment
INTEGER(I4B), INTENT(IN) :: n
REAL(DP), DIMENSION(n) :: arth_d
INTEGER(I4B) :: k,k2
REAL(DP) :: temp
if (n > 0) arth_d(1)=first
if (n <= NPAR_ARTH) then
  do k=2,n
    arth_d(k)=arth_d(k-1)+increment
  end do
else
  do k=2,NPAR2_ARTH
    arth_d(k)=arth_d(k-1)+increment
  end do
  temp=increment*NPAR2_ARTH
  k=NPAR2_ARTH
  do
    if (k >= n) exit
    k2=k+k
    arth_d(k+1:min(k2,n))=temp+arth_d(1:min(k,n-k))
    temp=temp+temp
    k=k2
  end do
end if
END FUNCTION arth_d

FUNCTION arth_i(first,increment,n)
INTEGER(I4B), INTENT(IN) :: first,increment,n
INTEGER(I4B), DIMENSION(n) :: arth_i
INTEGER(I4B) :: k,k2,temp
if (n > 0) arth_i(1)=first
if (n <= NPAR_ARTH) then
  do k=2,n
    arth_i(k)=arth_i(k-1)+increment
  end do
else
  do k=2,NPAR2_ARTH
    arth_i(k)=arth_i(k-1)+increment
  end do
  temp=increment*NPAR2_ARTH
  k=NPAR2_ARTH
  do
    if (k >= n) exit
    k2=k+k
    arth_i(k+1:min(k2,n))=temp+arth_i(1:min(k,n-k))
    temp=temp+temp
    k=k2
  end do
end if
END FUNCTION arth_i

FUNCTION geop_r(first,factor,n)
  Array function returning a geometric progression.
REAL(SP), INTENT(IN) :: first,factor

```

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```

INTEGER(I4B), INTENT(IN) :: n
REAL(SP), DIMENSION(n) :: geop_r
INTEGER(I4B) :: k,k2
REAL(SP) :: temp
if (n > 0) geop_r(1)=first
if (n <= NPAR_GEOP) then
  do k=2,n
    geop_r(k)=geop_r(k-1)*factor
  end do
else
  do k=2,NPAR2_GEOP
    geop_r(k)=geop_r(k-1)*factor
  end do
  temp=factor**NPAR2_GEOP
  k=NPAR2_GEOP
  do
    if (k >= n) exit
    k2=k+k
    geop_r(k+1:min(k2,n))=temp*geop_r(1:min(k,n-k))
    temp=temp*temp
    k=k2
  end do
end if
END FUNCTION geop_r

FUNCTION geop_d(first,factor,n)
REAL(DP), INTENT(IN) :: first,factor
INTEGER(I4B), INTENT(IN) :: n
REAL(DP), DIMENSION(n) :: geop_d
INTEGER(I4B) :: k,k2
REAL(DP) :: temp
if (n > 0) geop_d(1)=first
if (n <= NPAR_GEOP) then
  do k=2,n
    geop_d(k)=geop_d(k-1)*factor
  end do
else
  do k=2,NPAR2_GEOP
    geop_d(k)=geop_d(k-1)*factor
  end do
  temp=factor**NPAR2_GEOP
  k=NPAR2_GEOP
  do
    if (k >= n) exit
    k2=k+k
    geop_d(k+1:min(k2,n))=temp*geop_d(1:min(k,n-k))
    temp=temp*temp
    k=k2
  end do
end if
END FUNCTION geop_d

FUNCTION geop_i(first,factor,n)
INTEGER(I4B), INTENT(IN) :: first,factor,n
INTEGER(I4B), DIMENSION(n) :: geop_i
INTEGER(I4B) :: k,k2,temp
if (n > 0) geop_i(1)=first
if (n <= NPAR_GEOP) then
  do k=2,n
    geop_i(k)=geop_i(k-1)*factor
  end do
else
  do k=2,NPAR2_GEOP
    geop_i(k)=geop_i(k-1)*factor
  end do

```

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```

temp=factor**NPAR2_GEOP
k=NPAR2_GEOP
do
  if (k >= n) exit
  k2=k+k
  geop_i(k+1:min(k2,n))=temp*geop_i(1:min(k,n-k))
  temp=temp*temp
  k=k2
end do
end if
END FUNCTION geop_i
FUNCTION geop_c(first,factor,n)
COMPLEX(SP), INTENT(IN) :: first,factor
INTEGER(I4B), INTENT(IN) :: n
COMPLEX(SP), DIMENSION(n) :: geop_c
INTEGER(I4B) :: k,k2
COMPLEX(SP) :: temp
if (n > 0) geop_c(1)=first
if (n <= NPAR_GEOP) then
  do k=2,n
    geop_c(k)=geop_c(k-1)*factor
  end do
else
  do k=2,NPAR2_GEOP
    geop_c(k)=geop_c(k-1)*factor
  end do
  temp=factor**NPAR2_GEOP
  k=NPAR2_GEOP
  do
    if (k >= n) exit
    k2=k+k
    geop_c(k+1:min(k2,n))=temp*geop_c(1:min(k,n-k))
    temp=temp*temp
    k=k2
  end do
end if
END FUNCTION geop_c
FUNCTION geop_dv(first,factor,n)
REAL(DP), DIMENSION(:), INTENT(IN) :: first,factor
INTEGER(I4B), INTENT(IN) :: n
REAL(DP), DIMENSION(size(first),n) :: geop_dv
INTEGER(I4B) :: k,k2
REAL(DP), DIMENSION(size(first)) :: temp
if (n > 0) geop_dv(:,1)=first(:)
if (n <= NPAR_GEOP) then
  do k=2,n
    geop_dv(:,k)=geop_dv(:,k-1)*factor(:)
  end do
else
  do k=2,NPAR2_GEOP
    geop_dv(:,k)=geop_dv(:,k-1)*factor(:)
  end do
  temp=factor**NPAR2_GEOP
  k=NPAR2_GEOP
  do
    if (k >= n) exit
    k2=k+k
    geop_dv(:,k+1:min(k2,n))=geop_dv(:,1:min(k,n-k))*&
      spread(temp,2,size(geop_dv(:,1:min(k,n-k)),2))
    temp=temp*temp
    k=k2
  end do
end if

```

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```

END FUNCTION geop_dv

RECURSIVE FUNCTION cumsum_r(arr,seed) RESULT(ans)
    Cumulative sum on an array, with optional additive seed.
    REAL(SP), DIMENSION(:), INTENT(IN) :: arr
    REAL(SP), OPTIONAL, INTENT(IN) :: seed
    REAL(SP), DIMENSION(size(arr)) :: ans
    INTEGER(I4B) :: n,j
    REAL(SP) :: sd
    n=size(arr)
    if (n == 0_i4b) RETURN
    sd=0.0_sp
    if (present(seed)) sd=seed
    ans(1)=arr(1)+sd
    if (n < NPAR_CUMSUM) then
        do j=2,n
            ans(j)=ans(j-1)+arr(j)
        end do
    else
        ans(2:n:2)=cumsum_r(arr(2:n:2)+arr(1:n-1:2),sd)
        ans(3:n:2)=ans(2:n-1:2)+arr(3:n:2)
    end if
END FUNCTION cumsum_r

RECURSIVE FUNCTION cumsum_i(arr,seed) RESULT(ans)
    INTEGER(I4B), DIMENSION(:), INTENT(IN) :: arr
    INTEGER(I4B), OPTIONAL, INTENT(IN) :: seed
    INTEGER(I4B), DIMENSION(size(arr)) :: ans
    INTEGER(I4B) :: n,j,sd
    n=size(arr)
    if (n == 0_i4b) RETURN
    sd=0_i4b
    if (present(seed)) sd=seed
    ans(1)=arr(1)+sd
    if (n < NPAR_CUMSUM) then
        do j=2,n
            ans(j)=ans(j-1)+arr(j)
        end do
    else
        ans(2:n:2)=cumsum_i(arr(2:n:2)+arr(1:n-1:2),sd)
        ans(3:n:2)=ans(2:n-1:2)+arr(3:n:2)
    end if
END FUNCTION cumsum_i

RECURSIVE FUNCTION cumprod(arr,seed) RESULT(ans)
    Cumulative product on an array, with optional multiplicative seed.
    REAL(SP), DIMENSION(:), INTENT(IN) :: arr
    REAL(SP), OPTIONAL, INTENT(IN) :: seed
    REAL(SP), DIMENSION(size(arr)) :: ans
    INTEGER(I4B) :: n,j
    REAL(SP) :: sd
    n=size(arr)
    if (n == 0_i4b) RETURN
    sd=1.0_sp
    if (present(seed)) sd=seed
    ans(1)=arr(1)*sd
    if (n < NPAR_CUMPROD) then
        do j=2,n
            ans(j)=ans(j-1)*arr(j)
        end do
    else
        ans(2:n:2)=cumprod(arr(2:n:2)*arr(1:n-1:2),sd)
        ans(3:n:2)=ans(2:n-1:2)*arr(3:n:2)
    end if
END FUNCTION cumprod

```

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```

FUNCTION poly_rr(x,coeffs)
  Polynomial evaluation.
  REAL(SP), INTENT(IN) :: x
  REAL(SP), DIMENSION(:), INTENT(IN) :: coeffs
  REAL(SP) :: poly_rr
  REAL(SP) :: pow
  REAL(SP), DIMENSION(:), ALLOCATABLE :: vec
  INTEGER(I4B) :: i,n,nn
  n=size(coeffs)
  if (n <= 0) then
    poly_rr=0.0_sp
  else if (n < NPAR_POLY) then
    poly_rr=coeffs(n)
    do i=n-1,1,-1
      poly_rr=x*poly_rr+coeffs(i)
    end do
  else
    allocate(vec(n+1))
    pow=x
    vec(1:n)=coeffs
    do
      vec(n+1)=0.0_sp
      nn=ishft(n+1,-1)
      vec(1:nn)=vec(1:n:2)+pow*vec(2:n+1:2)
      if (nn == 1) exit
      pow=pow*pow
      n=nn
    end do
    poly_rr=vec(1)
    deallocate(vec)
  end if
END FUNCTION poly_rr

FUNCTION poly_dd(x,coeffs)
  REAL(DP), INTENT(IN) :: x
  REAL(DP), DIMENSION(:), INTENT(IN) :: coeffs
  REAL(DP) :: poly_dd
  REAL(DP) :: pow
  REAL(DP), DIMENSION(:), ALLOCATABLE :: vec
  INTEGER(I4B) :: i,n,nn
  n=size(coeffs)
  if (n <= 0) then
    poly_dd=0.0_dp
  else if (n < NPAR_POLY) then
    poly_dd=coeffs(n)
    do i=n-1,1,-1
      poly_dd=x*poly_dd+coeffs(i)
    end do
  else
    allocate(vec(n+1))
    pow=x
    vec(1:n)=coeffs
    do
      vec(n+1)=0.0_dp
      nn=ishft(n+1,-1)
      vec(1:nn)=vec(1:n:2)+pow*vec(2:n+1:2)
      if (nn == 1) exit
      pow=pow*pow
      n=nn
    end do
    poly_dd=vec(1)
    deallocate(vec)
  end if
END FUNCTION poly_dd

```

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```

FUNCTION poly_rc(x,coeffs)
COMPLEX(SPC), INTENT(IN) :: x
REAL(SP), DIMENSION(:), INTENT(IN) :: coeffs
COMPLEX(SPC) :: poly_rc
COMPLEX(SPC) :: pow
COMPLEX(SPC), DIMENSION(:), ALLOCATABLE :: vec
INTEGER(I4B) :: i,n,nn
n=size(coeffs)
if (n <= 0) then
  poly_rc=0.0_sp
else if (n < NPAR_POLY) then
  poly_rc=coeffs(n)
  do i=n-1,1,-1
    poly_rc=x*poly_rc+coeffs(i)
  end do
else
  allocate(vec(n+1))
  pow=x
  vec(1:n)=coeffs
  do
    vec(n+1)=0.0_sp
    nn=ishft(n+1,-1)
    vec(1:nn)=vec(1:n:2)+pow*vec(2:n+1:2)
    if (nn == 1) exit
    pow=pow*pow
    n=nn
  end do
  poly_rc=vec(1)
  deallocate(vec)
end if
END FUNCTION poly_rc

FUNCTION poly_cc(x,coeffs)
COMPLEX(SPC), INTENT(IN) :: x
COMPLEX(SPC), DIMENSION(:), INTENT(IN) :: coeffs
COMPLEX(SPC) :: poly_cc
COMPLEX(SPC) :: pow
COMPLEX(SPC), DIMENSION(:), ALLOCATABLE :: vec
INTEGER(I4B) :: i,n,nn
n=size(coeffs)
if (n <= 0) then
  poly_cc=0.0_sp
else if (n < NPAR_POLY) then
  poly_cc=coeffs(n)
  do i=n-1,1,-1
    poly_cc=x*poly_cc+coeffs(i)
  end do
else
  allocate(vec(n+1))
  pow=x
  vec(1:n)=coeffs
  do
    vec(n+1)=0.0_sp
    nn=ishft(n+1,-1)
    vec(1:nn)=vec(1:n:2)+pow*vec(2:n+1:2)
    if (nn == 1) exit
    pow=pow*pow
    n=nn
  end do
  poly_cc=vec(1)
  deallocate(vec)
end if
END FUNCTION poly_cc

FUNCTION poly_rrv(x,coeffs)

```

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```

REAL(SP), DIMENSION(:), INTENT(IN) :: coeffs,x
REAL(SP), DIMENSION(size(x)) :: poly_rrv
INTEGER(I4B) :: i,n,m
m=size(coeffs)
n=size(x)
if (m <= 0) then
  poly_rrv=0.0_sp
else if (m < n .or. m < NPAR_POLY) then
  poly_rrv=coeffs(m)
  do i=m-1,1,-1
    poly_rrv=x*poly_rrv+coeffs(i)
  end do
else
  do i=1,n
    poly_rrv(i)=poly_rr(x(i),coeffs)
  end do
end if
END FUNCTION poly_rrv

FUNCTION poly_ddv(x,coeffs)
REAL(DP), DIMENSION(:), INTENT(IN) :: coeffs,x
REAL(DP), DIMENSION(size(x)) :: poly_ddv
INTEGER(I4B) :: i,n,m
m=size(coeffs)
n=size(x)
if (m <= 0) then
  poly_ddv=0.0_dp
else if (m < n .or. m < NPAR_POLY) then
  poly_ddv=coeffs(m)
  do i=m-1,1,-1
    poly_ddv=x*poly_ddv+coeffs(i)
  end do
else
  do i=1,n
    poly_ddv(i)=poly_dd(x(i),coeffs)
  end do
end if
END FUNCTION poly_ddv

FUNCTION poly_msk_rrv(x,coeffs,mask)
REAL(SP), DIMENSION(:), INTENT(IN) :: coeffs,x
LOGICAL(LGT), DIMENSION(:), INTENT(IN) :: mask
REAL(SP), DIMENSION(size(x)) :: poly_msk_rrv
poly_msk_rrv=unpack(poly_rrv(pack(x,mask),coeffs),mask,0.0_sp)
END FUNCTION poly_msk_rrv

FUNCTION poly_msk_ddv(x,coeffs,mask)
REAL(DP), DIMENSION(:), INTENT(IN) :: coeffs,x
LOGICAL(LGT), DIMENSION(:), INTENT(IN) :: mask
REAL(DP), DIMENSION(size(x)) :: poly_msk_ddv
poly_msk_ddv=unpack(poly_ddv(pack(x,mask),coeffs),mask,0.0_dp)
END FUNCTION poly_msk_ddv

RECURSIVE FUNCTION poly_term_rr(a,b) RESULT(u)
  Tabulate cumulants of a polynomial.
REAL(SP), DIMENSION(:), INTENT(IN) :: a
REAL(SP), INTENT(IN) :: b
REAL(SP), DIMENSION(size(a)) :: u
INTEGER(I4B) :: n,j
n=size(a)
if (n <= 0) RETURN
u(1)=a(1)
if (n < NPAR_POLYTERM) then
  do j=2,n
    u(j)=a(j)+b*u(j-1)
  end do

```

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```

else
  u(2:n:2)=poly_term_rr(a(2:n:2)+a(1:n-1:2)*b,b*b)
  u(3:n:2)=a(3:n:2)+b*u(2:n-1:2)
end if
END FUNCTION poly_term_rr

RECURSIVE FUNCTION poly_term_cc(a,b) RESULT(u)
COMPLEX(SPC), DIMENSION(:), INTENT(IN) :: a
COMPLEX(SPC), INTENT(IN) :: b
COMPLEX(SPC), DIMENSION(size(a)) :: u
INTEGER(I4B) :: n,j
n=size(a)
if (n <= 0) RETURN
u(1)=a(1)
if (n < NPAR_POLYTERM) then
  do j=2,n
    u(j)=a(j)+b*u(j-1)
  end do
else
  u(2:n:2)=poly_term_cc(a(2:n:2)+a(1:n-1:2)*b,b*b)
  u(3:n:2)=a(3:n:2)+b*u(2:n-1:2)
end if
END FUNCTION poly_term_cc

FUNCTION zroots_unity(n,nn)
  Complex function returning nn powers of the nth root of unity.
  INTEGER(I4B), INTENT(IN) :: n,nn
  COMPLEX(SPC), DIMENSION(nn) :: zroots_unity
  INTEGER(I4B) :: k
  REAL(SP) :: theta
  zroots_unity(1)=1.0
  theta=TWOPI/n
  k=1
  do
    if (k >= nn) exit
    zroots_unity(k+1)=cplx(cos(k*theta),sin(k*theta),SPC)
    zroots_unity(k+2:min(2*k,nn))=zroots_unity(k+1)*&
      zroots_unity(2:min(k,nn-k))
    k=2*k
  end do
END FUNCTION zroots_unity

  Routines for "outer" operations on vectors. The order convention is: result(i,j) = first_operand(i)
  (op) second_operand(j).
FUNCTION outerprod_r(a,b)
REAL(SP), DIMENSION(:), INTENT(IN) :: a,b
REAL(SP), DIMENSION(size(a),size(b)) :: outerprod_r
outerprod_r = spread(a,dim=2,ncopies=size(b)) * &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerprod_r

FUNCTION outerprod_d(a,b)
REAL(DP), DIMENSION(:), INTENT(IN) :: a,b
REAL(DP), DIMENSION(size(a),size(b)) :: outerprod_d
outerprod_d = spread(a,dim=2,ncopies=size(b)) * &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerprod_d

FUNCTION outerdiv(a,b)
REAL(SP), DIMENSION(:), INTENT(IN) :: a,b
REAL(SP), DIMENSION(size(a),size(b)) :: outerdiv
outerdiv = spread(a,dim=2,ncopies=size(b)) / &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerdiv

FUNCTION outersum(a,b)
REAL(SP), DIMENSION(:), INTENT(IN) :: a,b

```

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```

REAL(SP), DIMENSION(size(a),size(b)) :: outersum
outersum = spread(a,dim=2,ncopies=size(b)) + &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outersum

FUNCTION outerdiff_r(a,b)
REAL(SP), DIMENSION(:), INTENT(IN) :: a,b
REAL(SP), DIMENSION(size(a),size(b)) :: outerdiff_r
outersdiff_r = spread(a,dim=2,ncopies=size(b)) - &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerdiff_r

FUNCTION outerdiff_d(a,b)
REAL(DP), DIMENSION(:), INTENT(IN) :: a,b
REAL(DP), DIMENSION(size(a),size(b)) :: outerdiff_d
outersdiff_d = spread(a,dim=2,ncopies=size(b)) - &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerdiff_d

FUNCTION outerdiff_i(a,b)
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: a,b
INTEGER(I4B), DIMENSION(size(a),size(b)) :: outerdiff_i
outersdiff_i = spread(a,dim=2,ncopies=size(b)) - &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerdiff_i

FUNCTION outerand(a,b)
LOGICAL(LGT), DIMENSION(:), INTENT(IN) :: a,b
LOGICAL(LGT), DIMENSION(size(a),size(b)) :: outerand
outerand = spread(a,dim=2,ncopies=size(b)) .and. &
  spread(b,dim=1,ncopies=size(a))
END FUNCTION outerand

  Routines for scatter-with-combine.
SUBROUTINE scatter_add_r(dest,source,dest_index)
REAL(SP), DIMENSION(:), INTENT(OUT) :: dest
REAL(SP), DIMENSION(:), INTENT(IN) :: source
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: dest_index
INTEGER(I4B) :: m,n,j,i
n=assert_eq2(size(source),size(dest_index),'scatter_add_r')
m=size(dest)
do j=1,n
  i=dest_index(j)
  if (i > 0 .and. i <= m) dest(i)=dest(i)+source(j)
end do
END SUBROUTINE scatter_add_r
SUBROUTINE scatter_add_d(dest,source,dest_index)
REAL(DP), DIMENSION(:), INTENT(OUT) :: dest
REAL(DP), DIMENSION(:), INTENT(IN) :: source
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: dest_index
INTEGER(I4B) :: m,n,j,i
n=assert_eq2(size(source),size(dest_index),'scatter_add_d')
m=size(dest)
do j=1,n
  i=dest_index(j)
  if (i > 0 .and. i <= m) dest(i)=dest(i)+source(j)
end do
END SUBROUTINE scatter_add_d
SUBROUTINE scatter_max_r(dest,source,dest_index)
REAL(SP), DIMENSION(:), INTENT(OUT) :: dest
REAL(SP), DIMENSION(:), INTENT(IN) :: source
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: dest_index
INTEGER(I4B) :: m,n,j,i
n=assert_eq2(size(source),size(dest_index),'scatter_max_r')
m=size(dest)
do j=1,n
  i=dest_index(j)

```

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```

        if (i > 0 .and. i <= m) dest(i)=max(dest(i),source(j))
    end do
END SUBROUTINE scatter_max_r
SUBROUTINE scatter_max_d(dest,source,dest_index)
REAL(DP), DIMENSION(:), INTENT(OUT) :: dest
REAL(DP), DIMENSION(:), INTENT(IN) :: source
INTEGER(I4B), DIMENSION(:), INTENT(IN) :: dest_index
INTEGER(I4B) :: m,n,j,i
n=assert_eq2(size(source),size(dest_index),'scatter_max_d')
m=size(dest)
do j=1,n
    i=dest_index(j)
    if (i > 0 .and. i <= m) dest(i)=max(dest(i),source(j))
end do
END SUBROUTINE scatter_max_d

Routines for skew operations on matrices:
SUBROUTINE diagadd_rv(mat,diag)
    Adds vector or scalar diag to the diagonal of matrix mat.
REAL(SP), DIMENSION(:,:), INTENT(INOUT) :: mat
REAL(SP), DIMENSION(:), INTENT(IN) :: diag
INTEGER(I4B) :: j,n
n = assert_eq2(size(diag),min(size(mat,1),size(mat,2)),'diagadd_rv')
do j=1,n
    mat(j,j)=mat(j,j)+diag(j)
end do
END SUBROUTINE diagadd_rv

SUBROUTINE diagadd_r(mat,diag)
REAL(SP), DIMENSION(:,:), INTENT(INOUT) :: mat
REAL(SP), INTENT(IN) :: diag
INTEGER(I4B) :: j,n
n = min(size(mat,1),size(mat,2))
do j=1,n
    mat(j,j)=mat(j,j)+diag
end do
END SUBROUTINE diagadd_r

SUBROUTINE diagmult_rv(mat,diag)
    Multiplies vector or scalar diag into the diagonal of matrix mat.
REAL(SP), DIMENSION(:,:), INTENT(INOUT) :: mat
REAL(SP), DIMENSION(:), INTENT(IN) :: diag
INTEGER(I4B) :: j,n
n = assert_eq2(size(diag),min(size(mat,1),size(mat,2)),'diagmult_rv')
do j=1,n
    mat(j,j)=mat(j,j)*diag(j)
end do
END SUBROUTINE diagmult_rv

SUBROUTINE diagmult_r(mat,diag)
REAL(SP), DIMENSION(:,:), INTENT(INOUT) :: mat
REAL(SP), INTENT(IN) :: diag
INTEGER(I4B) :: j,n
n = min(size(mat,1),size(mat,2))
do j=1,n
    mat(j,j)=mat(j,j)*diag
end do
END SUBROUTINE diagmult_r

FUNCTION get_diag_rv(mat)
    Return as a vector the diagonal of matrix mat.
REAL(SP), DIMENSION(:,:), INTENT(IN) :: mat
REAL(SP), DIMENSION(size(mat,1)) :: get_diag_rv
INTEGER(I4B) :: j
j=assert_eq2(size(mat,1),size(mat,2),'get_diag_rv')
do j=1,size(mat,1)
    get_diag_rv(j)=mat(j,j)

```

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```

end do
END FUNCTION get_diag_rv

FUNCTION get_diag_dv(mat)
REAL(DP), DIMENSION(:,,:), INTENT(IN) :: mat
REAL(DP), DIMENSION(size(mat,1)) :: get_diag_dv
INTEGER(I4B) :: j
j=assert_eq2(size(mat,1),size(mat,2),'get_diag_dv')
do j=1,size(mat,1)
  get_diag_dv(j)=mat(j,j)
end do
END FUNCTION get_diag_dv

SUBROUTINE put_diag_rv(diagv,mat)
  Set the diagonal of matrix mat to the values of a vector or scalar.
REAL(SP), DIMENSION(:), INTENT(IN) :: diagv
REAL(SP), DIMENSION(:,,:), INTENT(INOUT) :: mat
INTEGER(I4B) :: j,n
n=assert_eq2(size(diagv),min(size(mat,1),size(mat,2)),'put_diag_rv')
do j=1,n
  mat(j,j)=diagv(j)
end do
END SUBROUTINE put_diag_rv

SUBROUTINE put_diag_r(scal,mat)
REAL(SP), INTENT(IN) :: scal
REAL(SP), DIMENSION(:,,:), INTENT(INOUT) :: mat
INTEGER(I4B) :: j,n
n = min(size(mat,1),size(mat,2))
do j=1,n
  mat(j,j)=scal
end do
END SUBROUTINE put_diag_r

SUBROUTINE unit_matrix(mat)
  Set the matrix mat to be a unit matrix (if it is square).
REAL(SP), DIMENSION(:,,:), INTENT(OUT) :: mat
INTEGER(I4B) :: i,n
n=min(size(mat,1),size(mat,2))
mat(:,:)=0.0_sp
do i=1,n
  mat(i,i)=1.0_sp
end do
END SUBROUTINE unit_matrix

FUNCTION upper_triangle(j,k,extra)
  Return an upper triangular logical mask.
INTEGER(I4B), INTENT(IN) :: j,k
INTEGER(I4B), OPTIONAL, INTENT(IN) :: extra
LOGICAL(LGT), DIMENSION(j,k) :: upper_triangle
INTEGER(I4B) :: n
n=0
if (present(extra)) n=extra
upper_triangle=(outerdiff(arth_i(1,1,j),arth_i(1,1,k)) < n)
END FUNCTION upper_triangle

FUNCTION lower_triangle(j,k,extra)
  Return a lower triangular logical mask.
INTEGER(I4B), INTENT(IN) :: j,k
INTEGER(I4B), OPTIONAL, INTENT(IN) :: extra
LOGICAL(LGT), DIMENSION(j,k) :: lower_triangle
INTEGER(I4B) :: n
n=0
if (present(extra)) n=extra
lower_triangle=(outerdiff(arth_i(1,1,j),arth_i(1,1,k)) > -n)
END FUNCTION lower_triangle

```

Other routines:

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```
FUNCTION vabs(v)
    Return the length (ordinary  $L_2$  norm) of a vector.
    REAL(SP), DIMENSION(:), INTENT(IN) :: v
    REAL(SP) :: vabs
    vabs=sqrt(dot_product(v,v))
END FUNCTION vabs

END MODULE nrutil
```

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